













































**B. The Determinative Systems of Gliders**

The corresponding decimal code sets of determinative systems  $\mathcal{B}_j, j = 1, \dots, 6$  are presented.

1. For the glider  $a$ , the determinative system is

$$\mathcal{B}_1 == \left\{ \left\{ \begin{pmatrix} 0 & k_1 & 0 \\ k_1 & 0 & k_2 \\ 0 & k_2 & 0 \end{pmatrix} / \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} \right\}; \right. \\ \left. \left\{ \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} / \begin{pmatrix} k_2 & 0 & k_3 \\ 0 & k_3 & 0 \\ k_3 & 0 & k_4 \end{pmatrix} \right\} \right\},$$

$k_i = 0, n_1, n_2, n_3, n_4$  and  $i = 1, 2, 3, 4$ , where

$$\begin{aligned} n_1 &= 157\,301\,732\,472\,753\,487\,872, \\ n_2 &= 382\,914\,066\,129\,277\,157\,376, \\ n_3 &= 307\,109\,474\,942\,224\,171\,008, \\ n_4 &= 87\,838\,209\,750\,016\,720\,896. \end{aligned}$$

2. For the glider  $b$ , the determinative system is

$$\mathcal{B}_2 == \left\{ \left\{ \begin{pmatrix} 0 & k_1 & 0 \\ k_1 & 0 & k_2 \\ 0 & k_2 & 0 \end{pmatrix} / \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} \right\}; \right. \\ \left. \left\{ \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} / \begin{pmatrix} k_2 & 0 & k_3 \\ 0 & k_3 & 0 \\ k_3 & 0 & k_4 \end{pmatrix} \right\} \right\},$$

$k_i = 0, n_1, n_2, n_3, n_4$  and  $i = 1, 2, 3, 4$ , where

$$\begin{aligned} n_1 &= 1\,426\,112\,365\,437\,110\,779\,069\,669\,048\,320, \\ n_2 &= 1\,441\,199\,759\,666\,120\,901\,651\,836\,436\,480, \\ n_3 &= 71\,248\,204\,819\,881\,517\,263\,855\,747\,960\,355\,907\,987\,296\,380 \cdot \\ &\quad 518\,400, \\ n_4 &= 71\,248\,204\,820\,918\,315\,100\,583\,069\,735\,449\,887\,616\,897\,216 \cdot \\ &\quad 675\,840. \end{aligned}$$

3. For the glider  $c$ , the determinative system is

$$\mathcal{B}_3 == \left\{ \left\{ \begin{pmatrix} 0 & k_1 & 0 \\ k_1 & 0 & k_2 \\ 0 & k_2 & 0 \end{pmatrix} / \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} \right\}; \right. \\ \left. \left\{ \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} / \begin{pmatrix} k_2 & 0 & k_3 \\ 0 & k_3 & 0 \\ k_3 & 0 & k_4 \end{pmatrix} \right\} \right\},$$

$k_i = 0$ ,  $n_1, n_2$  and  $i = 1, 2, 3, 4$ , where

$$n_1 = 1\ 737\ 652\ 812\ 531\ 576\ 869\ 185\ 173\ 538\ 735\ 313\ 197\ 061\ 298': \\ 377\ 740\ 063\ 979\ 195\ 810\ 709\ 504,$$

$$n_2 = 107\ 839\ 992\ 356\ 672\ 231\ 205\ 423\ 157\ 951\ 804\ 061\ 011\ 470\ 513': \\ 723\ 684\ 758\ 003\ 267\ 634\ 462\ 720.$$

4. For the glider  $d$ , the determinative system is

$$\mathcal{B}_4 == \left\{ \left\{ \begin{pmatrix} 0 & k_1 & 0 \\ k_1 & 0 & k_2 \\ 0 & k_2 & 0 \end{pmatrix} / \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} \right\}; \right. \\ \left. \left\{ \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} / \begin{pmatrix} k_2 & 0 & k_3 \\ 0 & k_3 & 0 \\ k_3 & 0 & k_4 \end{pmatrix} \right\} \right\},$$

$k_i = 0$ ,  $n_1, n_2$  and  $i = 1, 2, 3, 4$ , where

$$n_1 = 162\ 264\ 707\ 324\ 156\ 913\ 662\ 044\ 271\ 542\ 272,$$

$$n_2 = 10\ 384\ 594\ 273\ 175\ 548\ 853\ 037\ 316\ 624\ 613\ 376.$$

5. For the glider  $e$ , the determinative system is

$$\mathcal{B}_5 == \left\{ \left\{ \begin{pmatrix} 0 & k_1 & 0 \\ k_1 & 0 & k_2 \\ 0 & k_2 & 0 \end{pmatrix} / \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} \right\}; \right. \\ \left. \left\{ \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} / \begin{pmatrix} k_2 & 0 & k_3 \\ 0 & k_3 & 0 \\ k_3 & 0 & k_4 \end{pmatrix} \right\} \right\},$$

$k_i = 0, n_1, n_2, n_3$  and  $i = 1, 2, 3, 4$ , where

$n_1 = 89\ 530\ 297\ 364\ 923\ 605\ 508\ 146\ 705\ 664\ 818\ 118\ 918\ 144,$

$n_2 = 539\ 231\ 843\ 434\ 284\ 405\ 901\ 976\ 779\ 735\ 939\ 138\ 261\ 719\ 529 \cdot$   
 $625\ 828\ 884\ 104\ 490\ 338\ 222\ 080,$

$n_3 = 539\ 231\ 843\ 434\ 159\ 220\ 014\ 183\ 401\ 125\ 745\ 276\ 163\ 384\ 563 \cdot$   
 $987\ 138\ 183\ 581\ 413\ 285\ 036\ 032.$

6. For the glider  $f$ , the determinative system is

$$\mathcal{B}_6 == \left\{ \left\{ \begin{pmatrix} 0 & k_1 & 0 \\ k_1 & 0 & k_2 \\ 0 & k_2 & 0 \end{pmatrix} / \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} \right\}; \right.$$

$$\left. \left\{ \begin{pmatrix} k_1 & 0 & k_2 \\ 0 & k_2 & 0 \\ k_2 & 0 & k_3 \end{pmatrix} / \begin{pmatrix} 0 & k_2 & 0 \\ k_2 & 0 & k_3 \\ 0 & k_3 & 0 \end{pmatrix} / \begin{pmatrix} k_2 & 0 & k_3 \\ 0 & k_3 & 0 \\ k_3 & 0 & k_4 \end{pmatrix} \right\} \right\},$$

$k_i = 0, n_1, n_2, n_3$  and  $i = 1, 2, 3, 4$ , where

$n_1 = 42\ 187\ 411\ 976\ 088\ 540\ 494\ 546\ 617\ 854\ 066\ 688,$

$n_2 = 1\ 098\ 980\ 723\ 400\ 879\ 481\ 039\ 162\ 633\ 706\ 099\ 850\ 677\ 091\ 041 \cdot$   
 $280,$

$n_3 = 1\ 673\ 237\ 945\ 072\ 905\ 942\ 430\ 424\ 223\ 935\ 627\ 264.$

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