

$\alpha = -2$ shows. The saturation behavior of the top nodes remains the same as it is for the Etch data. The convergence of ϕ toward a limit set by $\eta = 1$ is evident, with $\mu = -1$ as before. For the poorly linked nodes, the convergence is given by $\lambda = 0.35$. The other value that distinguishes the out-degree distribution in the Lenny release from that in the Etch release is $c \approx 90$. A solitary top node is to be seen for $x = 10\,446$.

To appreciate the mathematical implications of obtaining $\mu = -1$ from the data, a power-series expansion of equation (2) has to be carried out, leading to the infinite series,

$$\begin{aligned} \phi(x) = & \left(\frac{x+\lambda}{c}\right)^\alpha - \frac{\eta}{\mu} \left(\frac{x+\lambda}{c}\right)^{\alpha(\mu+1)} + \\ & \frac{\mu+1}{2} \left(\frac{\eta}{\mu}\right)^2 \left(\frac{x+\lambda}{c}\right)^{\alpha(2\mu+1)} + \dots, \end{aligned} \quad (3)$$

from which it is not difficult to see that a self-contained and natural truncation for this series can only be achieved when $\mu = -1$. This is necessary if the scale-free character of the distribution is to be preserved; otherwise, with $\mu \neq -1$, different terms in equation (3) will become dominant on different scales of x . It is remarkable that the Debian data conforms to this fact, and consequently, with $\mu = -1$, equation (1) is reduced to a linear, first-order, nonhomogeneous equation,

$$\frac{d\phi}{dx} - \left(\frac{\alpha}{x+\lambda}\right)\phi = -\left(\frac{\eta\alpha}{x+\lambda}\right), \quad (4)$$

in which η plays the role of a nonhomogeneity parameter.

With $\mu = -1$ (implying a power-law in the distribution) and with $\alpha = -2$ (implying that the power-law is specifically Zipf's law), the saturation properties of the network (for any value of η and λ) can be abstracted from equation (2) as

$$\phi(x) = \eta + \left(\frac{c}{x+\lambda}\right)^2. \quad (5)$$

One implication of the foregoing result is that nonhomogeneity in the system sets a firm lower bound to the number of rich nodes in the saturation regime, regardless of any arbitrarily high value of x ; that is, $\phi \rightarrow \eta$ as $x \rightarrow \infty$. In other words, nonhomogeneity defines a finite lower limit to the discrete count of the rich nodes. This clear deviation from the power-law model enables a few top nodes in the network of outgoing links to get disproportionately rich, as shown in Figures 2 and 4. All the links from these top nodes are outwardly directed toward the dependent nodes, making the presence of these

richly linked nodes an absolute necessity and burdening them with the responsibility of maintaining functional coherence in the FOSS distribution.

A scale for the onset of the saturation effects in the network of out-degree distributions can be found when the two terms in the right-hand side of equation (2) are in rough equipartition with each other. This will set a scale for the saturation of the number of links in the frequency distribution as

$$x_{\text{sat}} \approx \frac{c}{\sqrt{|\eta|}} - \lambda. \quad (6)$$

Considering the out-degree distribution in particular, it is always the case that $\eta = 1$. From the fitting function, noting that $\lambda \ll c$, we can also conclude that $x_{\text{sat}} \sim c$, a simple result that is useful in identifying the nodes that act as “hubs” and deviate from a scale-free distribution. All nodes with a number of links of the order of x_{sat} or greater will belong to this saturation regime. For the network of outgoing links, the Debian data indicates that approximately the top 1% of the nodes fall within this scale, with the package `libc6` being the most profusely connected node in all the releases.

The situation is quite the opposite for the network of incoming links, as Figures 1 and 3 show. Here the nodes draw in links to themselves, with all links being inwardly directed toward the nodes. This network of incoming links is complementary in character to the network of outgoing links. As a result, the richly linked nodes of the latter network are poorly connected in the former. In contrast to Figures 2 and 4, which indicate that the rich nodes serve the network to an extent that is disproportionately greater than what a simple power-law behavior would have required of them, we see from Figures 1 and 3 that the most richly linked nodes in the in-degree distribution display a behavior that falls short of what might be expected of a fully power-law trend (the top nodes here ought to have accreted more links if a power law only were to have been followed). So decreasing values of η over two generations of Debian releases show that for a given number of links x , the count of nodes ϕ is reduced. It is then clear that the ability of the top nodes to acquire links in the in-degree distribution becomes progressively weakened (and so it is that the deviation from the power-law behavior becomes sharper). Saturation in the network can also be quantitatively determined by the parameter η , which, when $\mu = -1$, appears as a nonhomogeneity condition in equation (1). The value and especially the sign of η afford us a precise means to distinguish the directed network of incoming links from that of outgoing links. The difference in the respective degree distributions in Figures 1 and 2 (or Figures 3 and 4) underscores this fact.

For small values of x , the poorly linked nodes also deviate from the power-law solution. This is especially true for the in-degree distribution in Figures 1 and 3. For small in-degree and out-degree distributions in the World Wide Web [31], an improved fit is obtained by a simple modification in the global power-law model [1, 27]. This type of modification can also be engineered in equation (5) to obtain a similar fit for the weakly linked nodes. In the limit of small degree distributions for both the in-directed and out-directed networks, where η ceases to have much significance, and where $x \sim 1$ (which, in the discrete count of links, is the lowest value that x can assume practically), an upper bound to the number of the sparsely linked nodes is found to be

$$\phi_{\text{ub}} \approx \left(\frac{c}{1 + \lambda} \right)^2, \quad (7)$$

with the full range of ϕ , therefore, going as $\eta \leq \phi \leq \phi_{\text{ub}}$.

4. Modeling Evolution and Saturation

Our model, based on two generations (Etch and Lenny) of a standard FOSS network (Debian), has shown that the saturation properties of the in-degree and the out-degree distributions are differently affected as time passes (marked by new releases of Debian). The degree distribution of the network of outgoing links shows no change when it comes to the model fitting of the top nodes (η maintains the same value). This is expected of these nodes. They form the foundation of the whole network, and their prime status continues to hold. In a semantic sense, meaning flows from these nodes to the derivative nodes. At the opposite end, the very poorly linked nodes in the outgoing network are fitted by changing values of λ (as shown in Figures 2 and 4). Again this is expected. In a mature and robust network, the possibility of semantic variations is much more open in the weakly linked derivative nodes, as opposed to the primordial nodes.

For the in-degree distributions, the situation is contrariwise. Going by Figures 1 and 3, the model fitting can be achieved properly by changing the value of η significantly. Further, with a new release of Debian, η actually decreases, a fact whose import is that the most richly linked nodes in the in-degree distribution (which are also the most-dependent nodes) acquire fewer links than they might have, if the power-law trend were to have been adhered to indefinitely. So, from a dynamic perspective, there is a limit up to which these dependent nodes continue to be linked.

Taking these observations together, we realize that the FOSS network is not a static entity. Rather it is a dynamically evolving network, as any standard software network is known to be [32, 33], undergoing continuous additions (even deletions) and modifications across several generations of Debian releases, contributed by the community of free-software developers. So any realistic model should account for this evolutionary aspect of the network distribution, and by now many theoretical models [34–37] have provided such insight into the dynamic evolution of networks. It is known too that scale-free networks emerge through the simultaneous operation of dynamic growth and preferential attachment [34, 38]. The limiting features of such a scale-free distribution ought also to come out naturally through the long-time dynamics.

The top nodes in the out-degree distribution form the irreducible nucleus of the FOSS network. These nodes are the most influential in the network. From the perspective of a continuum model, we look at the frequency distribution of the nodes in the network of outgoing links as a field $\phi(x, t)$ evolving continuously through time t with the saturation in the number of nodes for high values of x , emerging of its own accord from the dynamics. In keeping with this need, we frame an ansatz with a general power-law feature as

$$\phi(x, t) = \left(\frac{x + \lambda}{c} \right)^\alpha + \varphi(x, t), \quad (8)$$

in which $\varphi \rightarrow \eta$ as $t \rightarrow \infty$. This prescription is compatible with what equation (2) indicates when $\mu = -1$. Under this requirement, the temporal evolution of the network is described by a first-order, linear, nonhomogeneous equation, going as

$$\tau \frac{\partial \phi}{\partial t} = \frac{\partial \phi}{\partial x} - \frac{\alpha}{c^\alpha} (x + \lambda)^{\alpha-1}, \quad (9)$$

in which τ is a representative time scale on which the FOSS network evolves appreciably. Now equation (9) already has a power-law property built in it explicitly and is expected, upon being integrated under suitable initial conditions, to make the saturation features of the top nodes appear because of nonhomogeneity. This is the exact reverse of equation (4), which has nonhomogeneity explicitly designed in it, and upon being integrated, leads to a power-law behavior. The general solution of equation (9) can be obtained by the method of characteristics [39], in which we need to solve the equations

$$-\frac{dt}{\tau} = \frac{dx}{1} = \frac{d\phi}{\alpha(x + \lambda)^{\alpha-1} c^{-\alpha}}. \quad (10)$$

The solution of the $d\phi/dx$ equation is

$$\phi - \left(\frac{x + \lambda}{c}\right)^\alpha = a, \quad (11)$$

while the solution of the dx/dt equation is

$$x + \frac{t}{\tau} = b, \quad (12)$$

with both a and b being integration constants. The general solution is to be found under the condition that one characteristic solution of equation (10) is an arbitrary function of the other; that is, $a = f(b)$, with f having to be determined from the initial conditions [39]. So, going by the integral solutions given by equations (11) and (12), the general solution of $\phi(x, t)$ will be

$$f\left(x + \frac{t}{\tau}\right) = \phi - \left(\frac{x + \lambda}{c}\right)^\alpha, \quad (13)$$

which, under the initial condition that $\phi = \eta$ at $t = 0$, will characterize the profile of the arbitrary function f as

$$f(z) = \eta - \left(\frac{z + \lambda}{c}\right)^\alpha. \quad (14)$$

Hence, the specific solution can be obtained from equation (13) as

$$\phi(x, t) = \eta + \left(\frac{x + \lambda}{c}\right)^\alpha - \left[\frac{1}{c}\left(x + \lambda + \frac{t}{\tau}\right)\right]^\alpha, \quad (15)$$

and this, under the condition that $\alpha = -2$, will converge to the distribution given by equation (5), for $t \rightarrow \infty$. The significance of the initial condition is worth stressing here. For a value of x , the evolution starts at $t = 0$ with an initial node count of $\phi = \eta$, which, under all practical circumstances, is set at $\eta = 1$. This is to say that a node appears in the network with x number of links, where previously there existed no node with this particular number of links. As the network evolves, two things continue to happen: first, new nodes are added to the network, and second, already-existing nodes accrete links in greater numbers. The most heavily linked among the latter started as the primary nodes, and at $t = 0$, their number defines the minimum number of independent packages that are absolutely necessary for the FOSS network to evolve subsequently (for $t > 0$) into a robust semantic system. From a semantic perspective, the initial condition can be argued to have an axiomatic character, and the mature network burgeons from it on later time scales. And during the evolution, the entire

network gets dynamically self-organized in such a manner that the eventual static out-degree distribution has its saturation properties at the highly connected end determined by what the initial field was like at $t = 0$.

The asymptotic properties of equation (15) can now be examined, both in the limit of $t \rightarrow 0$ and in the limit of $t \rightarrow \infty$. In the former case, the evolution of ϕ will be linear in t for a given value of x and will go as

$$\phi(x, t) \simeq \eta - \alpha \frac{(x + \lambda)^{\alpha-1}}{c^\alpha} \left(\frac{t}{\tau} \right), \quad (16)$$

in which growth is assured only when $\alpha < 0$. This linearity of early growth reflects the assumption of a linear growth of the number of nodes with time [40].

While the temporal evolution obeys linearity on early time scales, in the opposite limit of $t \rightarrow \infty$, the evolution shifts asymptotically to a power-law trend going as

$$\phi(x, t) - \eta - \left(\frac{x + \lambda}{c} \right)^\alpha \simeq - \frac{1}{c^\alpha} \left(\frac{t}{\tau} \right)^\alpha. \quad (17)$$

Naturally, convergence toward a steady state, as it has been given by the condition in the left-hand side of the foregoing relation, will be possible only when $\alpha < 0$, a requirement that is satisfied by Zipf's law ($\alpha = -2$). Free and open-source software has been known to have its dynamic processes driven by power laws [20, 21], which is a clear sign that long memory prevails in this kind of system.

Now from the steady-state form of the degree distribution, as it is given by equation (2), we can set down for $\mu = -1$ a similar relation for the time-dependent field $\phi \equiv \phi(x, t)$ as

$$\phi(x, t) = \eta + \left(\frac{x + \tilde{\lambda}}{\tilde{c}} \right)^\alpha, \quad (18)$$

where $\tilde{\lambda}$ and \tilde{c} are "dressed" parameters, defined as $\tilde{\lambda} = \lambda \nu(x, t)$ and $\tilde{c} = c \zeta(x, t)$, respectively. The scaling form of the two functions ν and ζ can be determined by equating the right-hand sides of equations (15) and (18). This will lead to

$$\left(\frac{x + \tilde{\lambda}}{\tilde{c}} \right)^\alpha = \left(\frac{x + \lambda}{c} \right)^\alpha - \left[\frac{1}{c} \left(x + \lambda + \frac{t}{\tau} \right) \right]^\alpha. \quad (19)$$

For scales of $x \gg \lambda$ (typically $x \gtrsim 10$), a converging power-series expansion of increasingly higher orders of λ/x can be carried out with the help of equation (19). The zeroth-order condition will deliver

the scaling profile of ζ as

$$\zeta(x, t) = \left[1 - \left(1 + \frac{t}{x\tau} \right)^\alpha \right]^{-1/\alpha}. \quad (20)$$

This function bears time-translational properties, and at a given scale of x , it causes the degree distribution to shift across the x - ϕ plot through time. However, it is also not difficult to see that when $\alpha = -2$, there is a convergence toward $\zeta = 1$ (the steady state limit) as $t \rightarrow \infty$. And when $x \rightarrow \infty$, on any finite time scale, $\zeta \rightarrow 0$. This is why the count of the most heavily connected nodes (for which x has a high value) stays nearly the same ($\phi = \eta$) at all times, a fact that is borne out by the out-degree distributions in Figures 2 and 4. The saturation scale of x for such behavior is given by equation (6). A related fact that also emerges is that time-translation of the degree distribution becomes steadily more pronounced as we move away from $x \sim x_{\text{sat}}$ toward the lower limit of $x = 1$ (the least number of links that a node can possess). Consequently, as the temporal evolution progresses, the out-degree distribution assumes a slanted appearance, with a negative slope in the x - ϕ plane, something shown clearly in Figures 2 and 4. The model fitting in these two plots indicates that the value of c increases with time. This is how it should be, going by the form of the scaling function $\zeta(x, t)$, if we are careful to observe that c in both the plots is to be viewed as \tilde{c} , to account for its time-dependent variation.

Information regarding the time-translational properties of the poorly connected nodes is contained in the scaling function $\nu(x, t)$. However, a look at the left-hand side of equation (19) reveals that ν is coupled to ζ , and this nonlinear coupling causes complications. Going back to the power-series expansion in λ/x , as it can be obtained from equation (19), we may suppose that just as the zeroth-order in the series has yielded a proper scaling form for ζ , the higher orders in the series will bring forth a similar form for ν . And indeed we do obtain such a solution, going as $\nu^k = \zeta^\alpha [1 - (1 + t/x\tau)^{\alpha-k}]$, with k being the order of the expansion in the power series. But this result is misleading because the parameter λ and the scaling function $\nu(x, t)$ are influential only when $\lambda \gtrsim x$, with x assuming arbitrarily small values in the continuum model. Therefore, the correct approach here is not to take a series expansion in λ/x , but rather in x/λ , with a proper convergence of the series taking place for higher orders in x/λ . The zeroth-order term of this series gives the scaling form $\nu^\alpha = \zeta^\alpha [1 - (1 + t/\lambda\tau)^\alpha]$. The primary difficulty with this result is that the true functional dependence of ζ in this case is not known. This is certainly not going to be the function that is implied by equation (20), because this form of ζ is valid only on scales where $x \gg \lambda$.

Considering everything, the clear message derived from the common pattern exhibited by the two generations of out-degree distributions is that the value of λ has a significant bearing on the number of the preponderant but sparsely connected nodes, a fact that is described by equation (7). In the continuum picture of the degree distribution, λ is the theoretical lower bound of the number of links that the most weakly linked nodes may possess (which saves ϕ from suffering a divergence as $x \rightarrow 0$, as equation (5) shows). Through the evolutionary growth of the network, an increase in the value of λ suggests that these poorly linked nodes become incrementally relevant to the system by contributing more links in the out-directed network. Now these poorly connected nodes in the out-degree distribution are also the most profusely linked nodes in the in-directed network. Figures 1 and 3 show that for these nodes the value of η decreases with the evolution of the FOSS network. So while these nodes become progressively more relevant as members of the out-directed network (a condition quantified by increasing values of λ), as members of the in-directed network they become progressively less dependent (quantified by decreasing values of η). Analyzing the data of all the six generations of Debian, it is seen for the out-directed network that the value of λ remains nearly the same up to the fourth release, Etch, but grows noticeably thereafter for the next two releases, Lenny and Squeeze. Figures 5 and 6 show, respectively, the in-degree and the out-degree distributions of the release Squeeze.

In contrast, in the in-directed network, the value of λ grows quickly for the early releases and then saturates in the Lenny and Squeeze releases. Remembering that in the in-directed network the most poorly linked nodes are actually the parent nodes of the entire network, we conclude that even these nodes become dependent on other nodes to a small extent. Taken as a whole, as time increases, the interdependency character of the entire network becomes more firmly established, with even the relatively unimportant nodes showing a tendency to contribute outwardly directed links.

Quantitative support in favor of this claim comes from the dynamics of the out-directed network. In this case, the total number of nodes $N_{\text{out}}(t)$ at any given point of time t can be obtained by evaluating the integral

$$N_{\text{out}}(t) = \int_1^{x_m} \phi(x, t) dx. \quad (21)$$

The limits of this integral are decided by the limits on the number of links that the nodes possess, 1 being the lower limit and x_m being the upper (maximum) limit. The integral in equation (21) can be solved by taking the profile of $\phi(x, t)$ given by equation (15), for $\alpha = -2$.

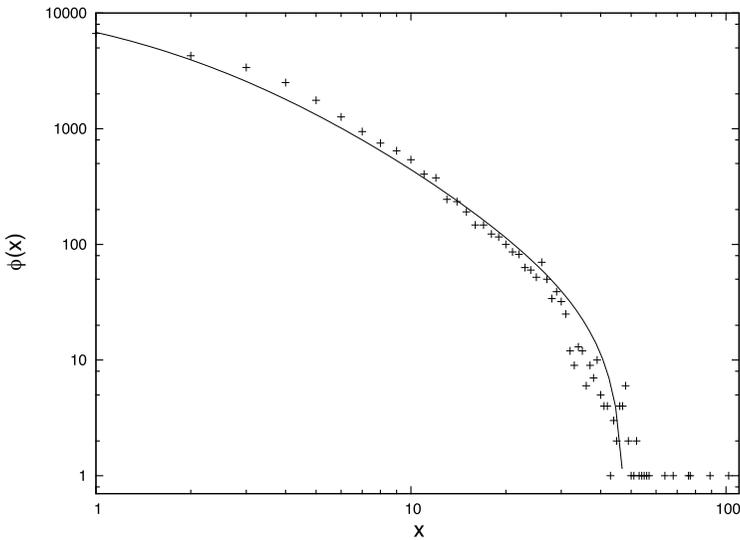


Figure 5. On large scales of x in the network of incoming links of the latest stable release, Squeeze, the saturation of the degree distribution is fitted by the parameter value $\eta = -28$. When x is small, the fit is obtained for $\lambda = 2.2$. For this plot, $c \approx 265$.

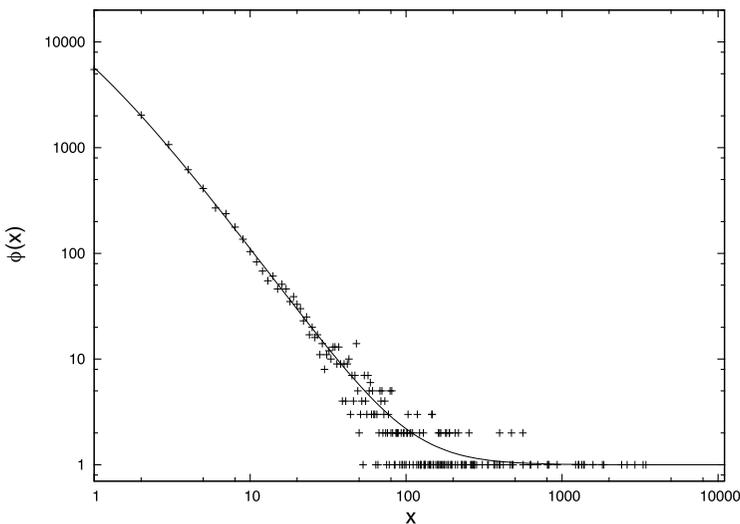


Figure 6. The out-degree distribution of the latest stable release, Squeeze, is in agreement with what the dynamic model predicts. The values of λ and c increase, as expected, to $\lambda = 0.45$ and $c \approx 110$. The richest node in this distribution has 12 470 links.

Noting that $x_m \gg 1$ (typically $x_m \sim 10^4$) for the out-directed network, the total number of nodes at any time can be estimated as

$$N_{\text{out}}(t) \simeq \eta x_m + \frac{c^2}{1 + \lambda} - c^2 \left(1 + \lambda + \frac{t}{\tau} \right)^{-1}. \quad (22)$$

On moderate time scales, the last two terms in the right-hand side of equation (22) are roughly equal. So the dominant contribution comes from the first term (the saturation term), as a consequence of which we can set down $N_{\text{out}} \sim x_m$. This argument becomes progressively more correct for large values of x_m , that is, for later releases of Debian.

For the out-degree distribution in the Etch release, $x_m \simeq 9000$, while in the Lenny release, the corresponding number is about 10 000. Using these values from both the releases of Debian, the respective count of N_{out} can be made for the two successive generations. These values of N_{out} represent the number of nodes that contribute at least one link in the out-directed network. In the case of the Etch release, the number of software packages contributing to the out-directed network is counted to be about 8700 (which is closely comparable to the estimated value of $N_{\text{out}} \sim x_m \simeq 9000$), and in the case of the Lenny release, the total count of the out-directed nodes is about 11 000 (which can be favorably compared once again to $N_{\text{out}} \sim x_m \simeq 10\,000$). As a fraction of the total number of nodes, these actual counts indicate that the number of nodes in the out-directed network increases by 0.3% from the Etch release to the Lenny release. This validates the contention that with each passing generation, the network becomes incrementally more robust in terms of out-degree contributions coming from an increasingly greater number of nodes. The values pertaining to the latest stable release, Squeeze, also go along with this trend. In this case the actual count of the out-directed nodes is about 14 000, a number that is again comparable with the estimate of $N_{\text{out}} \sim x_m \simeq 12\,000$. In keeping with the predicted trend, the fraction of nodes contributing out-directed links in this release increases by 1.2%. We also note with curiosity that in these last three Debian releases, Etch, Lenny, and Squeeze, the total number of software packages in both the in-directed and out-directed networks is roughly twice the value of x_m in the out-directed network.

The overall growth of the network, however, slowly grinds to a halt on long time scales. This conclusion cannot be missed in equation (22), which suggests that the total number of nodes increases with time, but approaches a finite stationary value when $t \rightarrow \infty$, with x_m remaining finite. This inclination of the network to saturate toward a finite-size end can be explained in terms of the finite semantic

possibilities associated with each of the nodes. The extent of making creative use of the existing semantic possibilities of even the most intensely linked of the top nodes is limited. Since most of the nodes in the network depend on such top nodes, there must then be a terminal stage in the growth of the network. Unless novel creative elements in semantic terms are continuously added to the top nodes, the value of x_m will remain constrained within a certain bound, and saturation will happen. So saturation in the network is a consequence of the limit to the various ways in which original functions in the top nodes can be invoked by the derivative nodes. An illustration of this argument is to be seen in Figure 7, which plots actual values taken from all the Debian releases. This plot tracks the growth of the total number of nodes in the out-directed network. All the members of this network contribute at least one out-directed link, and so meaning (the semantic context) is seen to flow out of these nodes. Therefore, these nodes are the bearers of original axioms. That the growth of this entire out-directed network saturates toward a limiting value for the

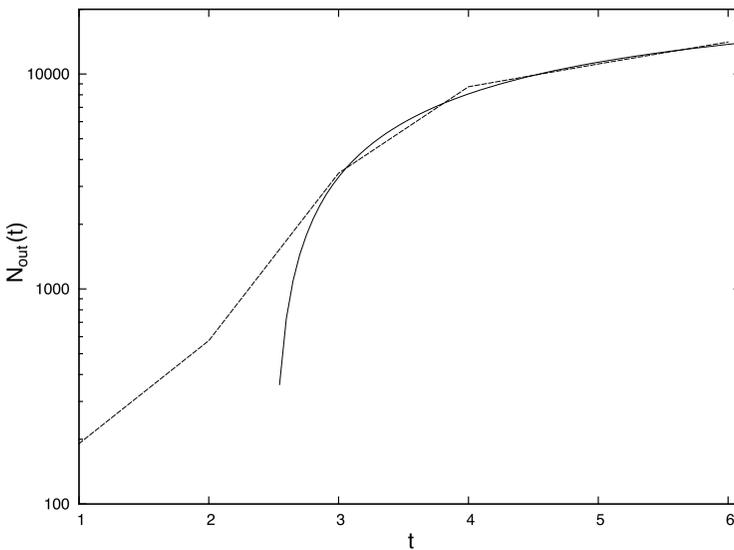


Figure 7. The broken dotted curve plots the growth of the total number of nodes in the out-directed network over six generations of Debian. The continuous curve, following equation (23), gives the fitting function of the data points. The fit, indicating a power-law approach toward saturation, agrees well for the later releases of Debian (the third release onward). In this plot t is a scaled time, marking the generation number. The parameter values are $A = 29\,000$, $B = 113\,000$, and $C = 1.4$, which are compatible when viewed in terms of η , λ , c , and x_m , as they have been set in Figures 2, 4, and 6.

later releases of Debian is quite obvious from the trend indicated in Figure 7. The data curve is fitted by a general form of equation (22), going as

$$N_{\text{out}}(t) \simeq A - \frac{B}{C + t}, \quad (23)$$

where $A = \eta x_m + c^2 (1 + \lambda)^{-2}$, $B = c^2 \tau$, and $C = (1 + \lambda) \tau$. The implication of the foregoing expression is that the long-time approach toward the terminal stage in the growth of the network is like a power law. From the fitting function, this looks very much true for the later releases of Debian. Now saturation in the growth of the axiom-bearing nodes (with out-directed links) means that the growth of the network of in-directed nodes will also saturate in tandem. The semantic flow in the entire network terminates at these nodes, and as such these “terminal” nodes are also indicators of saturation.

5. Concluding Remarks

This work is based on the networks of direct dependencies in the component-based software Debian. A deeper understanding of dependency-based semantic features can be had on introducing the notions of strong dependencies and package sensitivity, which are instrumental in distinguishing transitive dependencies from conjunctive and disjunctive dependencies [23]. We note that direct and strong dependencies generally tend to be correlated [23]. These features may have a bearing on redundancy in the operating system and its robustness against failure. We may also mention in passing that network structures in component-based software are determined by specific fields, with “depends,” which is the basis of this study, being just one of such fields (“conflicts,” for instance, being another). A particular field may give rise to specific features in the network, characteristic of itself only.

The mathematical model developed in this work makes a quantitative distinction between the incoming and outgoing distributions in the Debian GNU/Linux network. Similar features are known to exist in the degree distributions of other scale-free networks, and with the mathematical framework applied here, it should become possible to study the saturation properties and the specific directional characteristics of scale-free networks in general. To take an example, the degree distributions of the World Wide Web and Debian appear to be the converse of each other. And so what looks like an in-degree distribution for one is the out-degree distribution for the other, and vice

versa [1]. The model provided here is general enough to capture the specific features of the two different cases by a suitable tuning of the parameters.

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